

WEPD – Type I [68, 34, 12]

This is a database of known weight enumerator parameters for singly-even binary self-dual [68, 34, 12] codes.

The possible weight enumerators of a singly-even binary self-dual [68, 34, 12] code are given in [2] as

$$\begin{aligned}W_{68,1} &= 1 + (442 + 4\alpha)x^{12} + (10864 - 8\alpha)x^{12} + \dots, \\W_{68,2} &= 1 + (442 + 4\alpha)x^{12} + (14960 - 8\alpha - 256\beta)x^{12} + \dots,\end{aligned}$$

where $\alpha, \beta \in \mathbb{Z}$.

See the links below for lists of known values of (α, β) for $W_{68,1}$ and $W_{68,2}$.

- [W_{68,1} known parameters](#) (from [4, 5, 20, 23, 24, 26, 30, 31, 38–41])
- [W_{68,2} known parameters](#) (from [1–23, 25–37, 39–41])

References

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